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Design space exploration in embodiment design: an application to the design of aircraft air conditioners

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Abstract: The embodiment design of aeronautic systems proves to be a difficult design phase due to the variability in the system environment; the design is often constrained by atmospheric conditions. These atmospheric conditions appear to be highly variable according to the flight phases of the aircraft.

The difficulty when designing air-conditioning systems for civil aircrafts is also inherent to the complexity of the coupling of the non linear physical phenomena inside of these systems (multi-physics, multi-scaling). Therefore, the design space appears to be very broad and quite difficult to explore. Embodiment design choices are relating to continuous and discrete design variables while the system effectiveness is extremely sensitive to most of these design variables. There is a lack of tools to support the investigation of the design exploration space and designer decisions at early stages of the design process. In this paper, a method is proposed to generate feasible embodiments and manage the compromise between various design requirements.

A digital tool based on the meta-heuristic of Genetic Algorithms (Gas) has been developed to investigate the design problem. The selection of non-dominated solutions (Pareto) is used to identify relevant values for design variables and to facilitate choices among the design solutions of the air conditioning system.

Keywords: design space exploration; embodiment design; genetic algorithm; trade-off; nondominated solutions; Pareto; decision support; bootstrap; aeronautics.

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1 Embodiment design of complex systems

1.1 Research context

Before the detail design phase, the embodiment design phase leads to the definition of a design configuration where the main dimensions and components are chosen (Pahl and Beitz, 1996). This design phase remains challenging in the context of industrial design departments. Indeed, at a stage where the knowledge is uncertain, most of the existing computer-aided tools are not suitable because they are based on models requiring the complete geometrical definition of the product. Designers do not have tools to support them in making decisions. The decisions regarding the choice of concepts are based on the assessment of performances (O'Sullivan, 2001). Therefore, many *a priori* choices are performed according to the expertise of the designer or of the company; these choices hide a great part of the potential solution space.

Embodiment design problems can be naturally expressed as mixed Constraint Satisfaction Problems (CSPs) (Scaravetti, 2004; Thornton, 1996), which cannot be solved using classical mechanical simulation tools. In order to overcome this difficulty, embodiment design problems are tackled using several solving strategies.

An overview of these solving strategies is presented by Antonsson and Cagan (2001). The existing tools are mainly concerned with genetic algorithm, evolutionary programming, agent-based systems and ensemblist methods (Chenouard *et al.*, 2007). These tools are developed for application relating to structural configuration in mechanics, microsystem and robotic synthesis, and chemical processes (Hugget *et al.*, 1999).

1.2 Application: airconditioning system design

This work is carried out in cooperation with Dassault Aviation, which is developing decision support tools for preliminary design.

Airconditioning systems for civil aircraft are made of several complex components which interact to regulate the air temperature and pressure in the cabin (Pérez-Grande and Leo, 2002). The system considered in this paper (see Figure 1) is a Joule-Brayton cycle-based airconditioning system (bootstrap). It is mainly made up of two cross-flow

Thanks to the discrete nature of some Design Variables (DVs) and to the discernment precision of the others, the number of solution principles of the design problem can be assessed. For example, the dimensions of the inlet sections of the two heat exchangers along two axes belong to continuous domains. However, they are related to discernment

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precision (minimum distance between two values of the variables regarded as different values). The domains of these dimensions range from one 0.01 m to 0.5 m. Their discernment precision has been defined by designers at 0.01 m. Thus, the number of combinations of distinct domains for these variables is equal to 2500 (50^2).

The size of the global bootstrap design problem has been assessed at approximately $1.04 \cdot 10^{15}$ design configurations when considering all of the possible value combinations of the DVs. However, not every design configuration corresponds to a design solution. Not every design configuration fits the design requirements and some design configurations do not work for some system environment conditions.

Moreover, the air-conditioning system has to supply air at constant temperature and pressure to the aircraft cabin. Therefore, the design of the bootstrap must take into account different flight phases corresponding to different altitudes and the relative speed of the aircraft. The temperature, pressure and relative speed of the air strongly vary between these flight points.

1.3 Embodiment design difficulties and proposal

Due to the complex interactions of the components, air-conditioning designers have low support to guide them in the process of determining the more efficient fin types inside the heat exchangers. Manual (as opposed to digital) solving processes require knowing the values of the DVs. Therefore, bootstrap designers usually give *a priori* values for the heat exchanger efficiencies, which is equivalent to considering one configuration of a heat exchanger without considering the variability of the design problem.

Designers frequently develop spreadsheets dedicated to specific issues, but few tools are available to assist them during this design phase, especially because the product behaviour modelling has to take into account complex combinations of physical phenomena. Moreover, design solution validation is performed as soon as all of the architectural choices are made. It is usually processed by developing a digital simulation code of an air-conditioning system and by testing and comparing the performances of a small number of configurations. Finally, the dimensioning of the system is performed for the most critical life cycle stage, the prevailing situation. Using a trial and error mode, designers converge towards a solution which is not necessarily the most powerful one, or which does not necessarily correspond to the best trade-off between the various flight phases.

The approach proposed in this paper leads to the identification of the best design compromises between various design objectives, whatever the life cycle stage. It consists of:

- the expression of the design problem as a set of constraints
- the exploration of the whole design space using Genetic Algorithms (GAs)
- the assessment of their performances using criteria relating to the design objectives
- the reduction of the solution space using the Pareto front: it allows the identification of solutions which are the best compromise in simultaneously satisfying the design objectives, without favouring one objective.

Until the end of the embodiment design phase, no potential solutions have been dismissed by any choice of the designer. The results of the approach proposed in this paper allow decision support at this stage of the design process.

2 Design problem modelling

2.1 Constraint modelling

In order to avoid the usual trial and error iterative design process and to not dismiss a solution because of *a priori* choices, we propose to simultaneously take all the constraints into consideration, without any hierarchy or preliminary choices, by modelling the problem as a set of constraints.

The relations linking the variables (equalities, inequalities, logical rules) and their domains of evaluation are the constraints of the design problem. Variables can be real numbers, integers or enumerated values. Parameter values of standard components can be described using discrete variables. Domain use is well adapted to the uncertain knowledge inherent to the embodiment design phase.

The variables which define the product architecture to be designed (dimension, standard component characteristics, materials, number of elements, *etc.*) are the DVs. The assessment of a solution is performed by using the criteria relating to the design objectives (Scaravetti *et al.*, 2006b): the resolution allows the evaluation of various working structures meeting the working conditions of the system. These solutions may be numerous and may thus need to be classified. In order to objectify the choices among these solutions, criteria which express the performance of each design configuration are used.

Consequently, a design problem is described by a set of DVs, criteria and constraints. A solution corresponds to a set of values – for all DVs and criteria – which meets all the stated constraints. These values define a particular design configuration.

2.2 Modelling of the design problem of the air-conditioning system

A methodology has been proposed to identify the structuring characteristics of the embodiment design problem, which must be translated into constraints (Scaravetti *et al.*, 2005a). The knowledge base of the air-conditioning system consists of:

- twenty-three thermodynamic state variables (pressures, mass flow rates, temperatures, *etc.*)
- fourteen geometric and structural variables (lengths, surface types, pass number, *etc.*)
- eight criteria (outputs, efficiencies, *etc.*) which define the performance or which are used to qualify the quality of a design configuration
- twenty-four auxiliary variables which are defined as functions which correlate their definitions with the 45 preceding variables.

The global model is constituted by 69 constraints. Constraints relating to physics have been derived from energy, momentum or mass flow conservation laws. Due to the complexity of the physical models, which indicates strongly coupled physical phenomena, model reduction methods have been applied (Scaravetti *et al.*, 2006b). The

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model of the design problem also includes the functional performance specifications and the description of standard components. The aircraft manufacturer expresses technical skills and manufacturing rules.

The DVs are:

- the type of fin (integer value ranging from 1 to 48)
- the dimensions of each exchanger (from 0.1 m to 0.5 m, with a discernment precision of 0.01 m)
- the diameter of the bypass pipes.

The performance criteria are:

- the mass of the heat exchangers
- the total volume of the two exchangers
- the drag force induced on the aircraft by the air-conditioning system, which can be negative when the system is providing thrust.

The system has to deliver air at constant temperature and pressure to the cabin whatever the flight phase (ground, lift, economic cruise, economic cruise for long haul flights, descent, *etc.*). The four main flight phases (see Table 1) have been included in the model of the design problem and investigated in this paper.

Table 1 Flight phase characteristics

<i>Aircraft speed</i>	<i>Altitude</i>	<i>Atm. pressure</i>	<i>Atm. temperature</i>
<i>Mach number</i>	<i>M</i>	<i>Pa (10⁴)</i>	<i>K</i>
0.8	11 000	2.272	216.7
0.5	3000	7.028	268.7
0.4	2000	7.967	275.2
0.6	5000	5.418	255.7

3 Generation of design configurations using a genetic algorithm

A first investigation of the design search space was carried out using a CSP solver (Scaravetti *et al.*, 2006a; Sébastien *et al.*, 2007). Only one flight point was investigated at this stage. More to the point, the bootstrap design problem was solved by considering only six kinds of fins inside the heat exchangers, whereas in this paper, 48 different types of fins and four different flight points have been considered. In this paper, several different life cycle situations (flight points) are taken into account, leading to a much more complex design space. Some solutions appear to be effective regarding several life cycle situations, whereas some others are only effective for one life cycle situation. Our approach has been extended by discriminating solutions according to DV values, in order to highlight relevant combinations of DVs. The most relevant solutions belong to the Pareto front and are effective for several flight points.

In the following paragraphs, the computing times of every exploration job have been limited to one hour of Central Processing Unit (CPU) time, in order to facilitate the comparison of the results. A GA-based design code has been developed to improve the solving performance of the bootstrap design problem process. The GA heuristic is a metaheuristic with a large scope of interest and applications (Diveux *et al.*, 2001; Hugget *et al.*, 1999). It is based on the mutation, crossover and selection of individuals from an evolving population. Evolving generations tend to improve an optimisation criterion (the fitness function) by mixing individual genes and generating random individuals to search the complete exploration space of solutions. This heuristic method is involved in many different types of mechanical design tools. However, in industrial conditions, it is mainly used as an optimisation tool for the management of several simulation codes. Simulation codes simulate the behaviour of different parts of the mechanical system, whereas the GA-based optimisation tool supervises the system architecture and the design performance criteria.

The design code proposed in this paper is used to solve a design CSP, rather than optimising a design problem. This means that the design code conducts a search for sets of solutions rather than optimised solutions. This is performed using an optimisation criterion guaranteeing the satisfaction of every constraint of the design problem. Every constraint ' C_i ' of the problem is related to a value ' $SAT(C_i)$ ': if C_i is satisfied, $SAT(C_i) = 1$, else $SAT(C_i) = 0$. The fitness function optimised by the GA is described in Equation (1):

$$SAT = \prod_{i=1}^n \frac{SAT(C_i) + 1}{2}. \quad (1)$$

The solutions considered in the following paragraphs satisfy every constraint of the problem ($SAT = 1$). The population size has been fixed to 100 individuals (candidate solutions) and the crossover probability is 0.5.

Due to the extreme sensitivity of the system functioning to the DV values (chiefly the selection of the heat exchanger fins), the mutation probability of the GA proves to be a key parameter of the solving process. A pure random search-based algorithm leads to relevant results (the design space is almost completely explored) but the computation times are high (Scaravetti and Sébastien, 2007). As a consequence, we take into consideration several values of the mutation probability, ranging from low values to very high values. In this paper, three different mutation probabilities are considered. The variable Mp equals 0.1 (Mp1), 0.3 (Mp3) or 0.6 (Mp6). Figure 2 highlights solutions minimising the performance criteria for each Mp. This selection was obtained by computing the set of nondominated solutions according to a Pareto method (see Section 4.1).

Figure 2 displays all the nondominated sets of solution spaces obtained for the three values of the mutation probability. Every solution is represented according to three performance criteria: the global mass and the volume of the heat exchangers, and the drag force induced. Figure 3 shows the same three sets on a 3D space. We note that the reading of the projections is easier.

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Figure 2 Pareto sets of solution spaces obtained for each mutation probability, displayed among performance criteria pair by pair

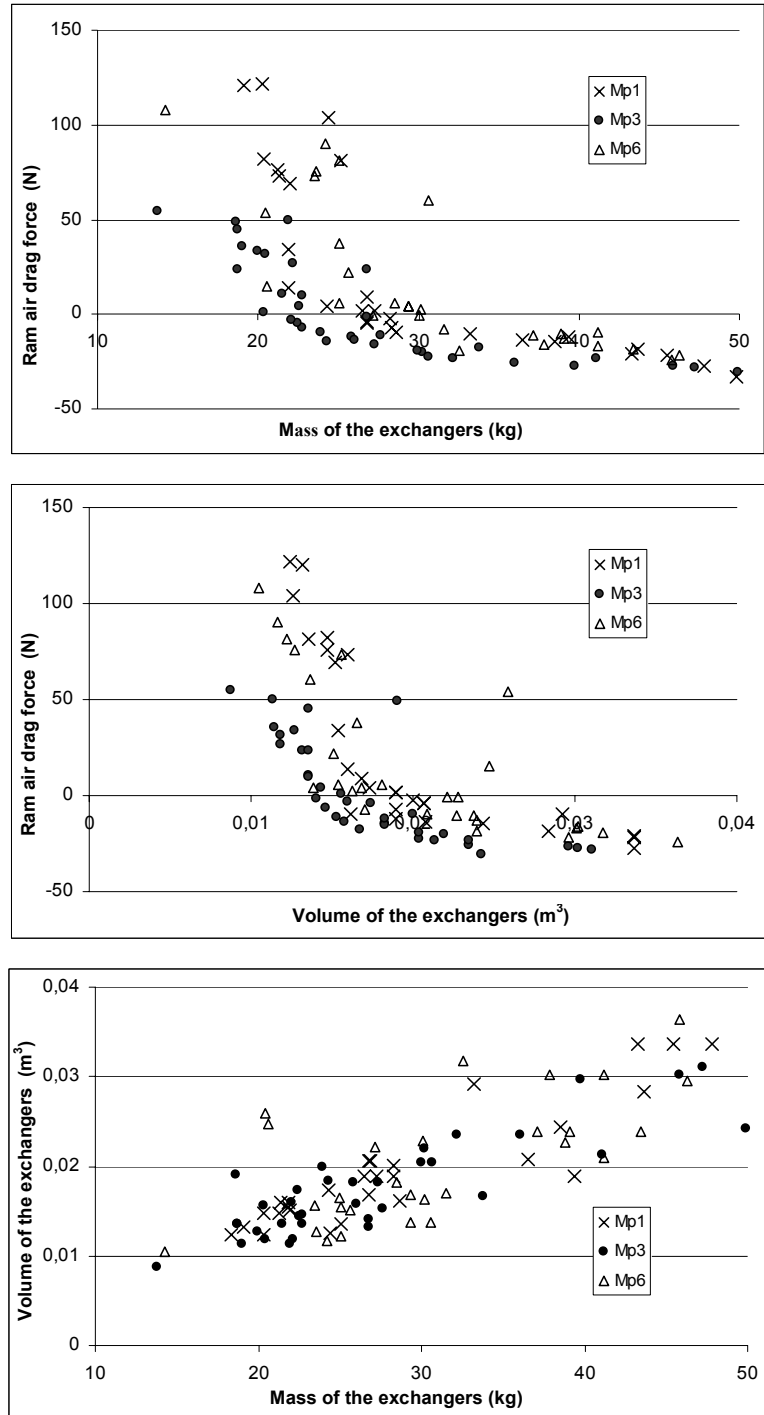
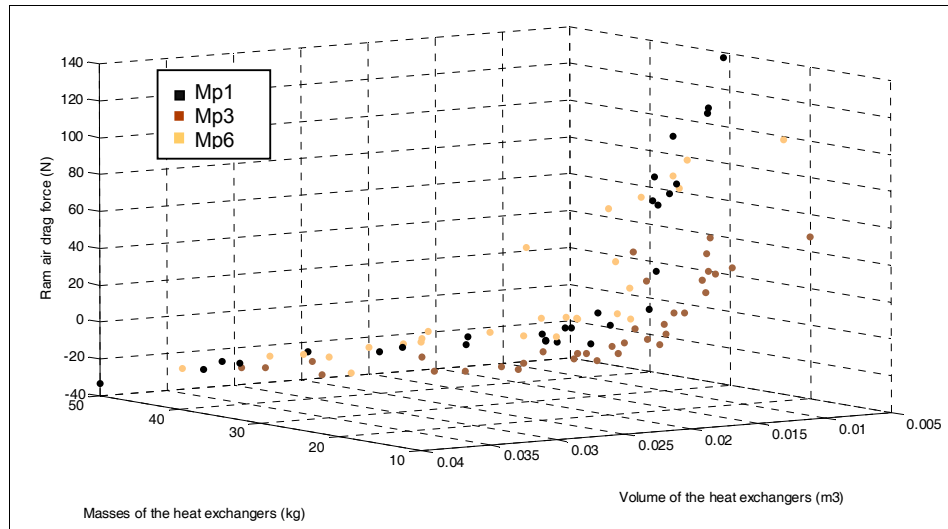


Figure 3 Three-dimensional Pareto fronts of solution spaces obtained for each mutation probability (3D display) (see online version for colours)



Each mutation probability leads to a different solution space, which performances are quite different. In the continuation of the paper, only the value $Mp = 0.3$ is considered in order to limit the size of the data exploitation and to better show the use of visualisation of relevant DV values.

4 Design space exploration

Once the investigation of the design configurations has been performed, we aim to support the decision of the designers by guiding the exploitation of the results. This means:

- guiding the choice of DVs among the variables of the problem by finding the relevant DVs or the relevant combinations of variables
- supporting decisions by reducing the solution space and finding suitable solutions.

4.1 Solution space reduction

The types of fins and the arrangement of the stacked plates in the heat exchangers have a decisive influence on the mass and the volume of the system. They also affect the efficiencies of the exchangers and therefore the air-conditioning efficiency of the system. Moreover, some of the air feeding the conditioning systems is scooped off the surface of the aircraft using a scoop. This air bleeding induces a drag force at the surface of the aircraft, which is detrimental to the global performance of the aircraft. This drag force has to be minimised. Therefore, a compromise has to be found between these antagonistic requirements.

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The solution classification has been investigated with an objective function (Scaravetti *et al.*, 2005a), but a weight factor-based method raises the problem of the value assignment of the weight factors.

Every Pareto solution is nondominated (Goldberg, 1989) and the front definition aims at minimising the performance criteria values. The selected solutions correspond to a trade-off between disparate and conflicting design performances (Hamdi *et al.*, 2006). A solution is nondominated if no other solution relates to the best values for all criteria (mass, volume and drag induced in our case).

The reduction of the solution space is quite efficient. Table 2 displays the sizes of the solution spaces and Pareto sets. This selection process drops the number of solutions from 2634 solutions to 35 solutions ($Mp = 0.3$). Less than 1% of the complete solution space (considering all Mp 's) belongs to the front (nondominated solutions).

Table 2 Number of solutions according to the mutation probability

	$Mp\ 1$	$Mp\ 3$	$Mp\ 6$	All Mp 's
Nb solutions	2325	2634	677	5636
Nb sol. Pareto set	29	35	28	37
	1.25%	1.33%	4.13%	0.66%

Figures 4 to 6 display the solutions in the performance space and locate the Pareto solutions matching the performance criteria pair by pair. A solution minimising two performance criteria may be detrimental to the third performance criterion. For instance, the solution corresponding to a mass of 13.8 kg is the Pareto solution according to the masses and volumes of the heat exchanger, but is detrimental to the drag force.

Figure 4 Performance space (volume versus drag force) and Pareto set

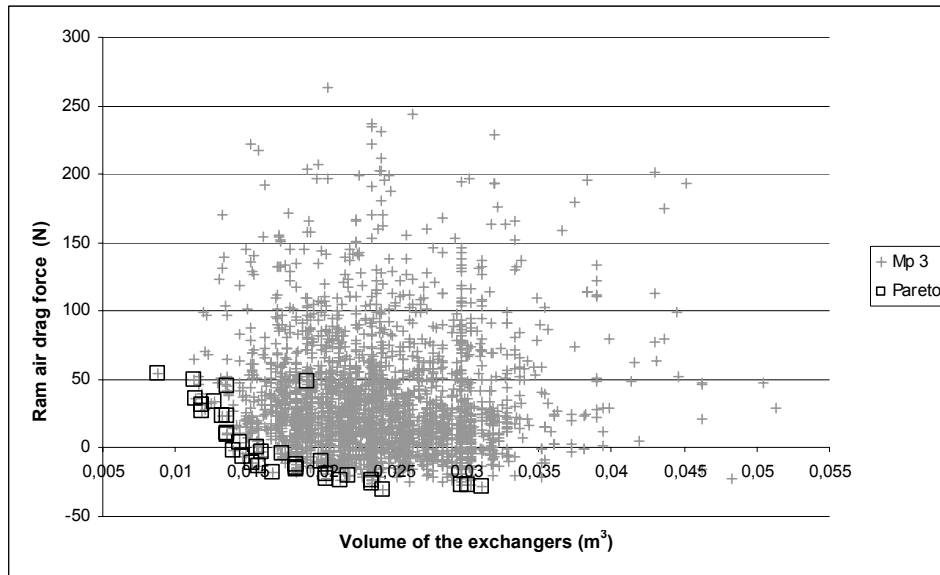


Figure 5 Performance space (mass versus drag force) and Pareto set

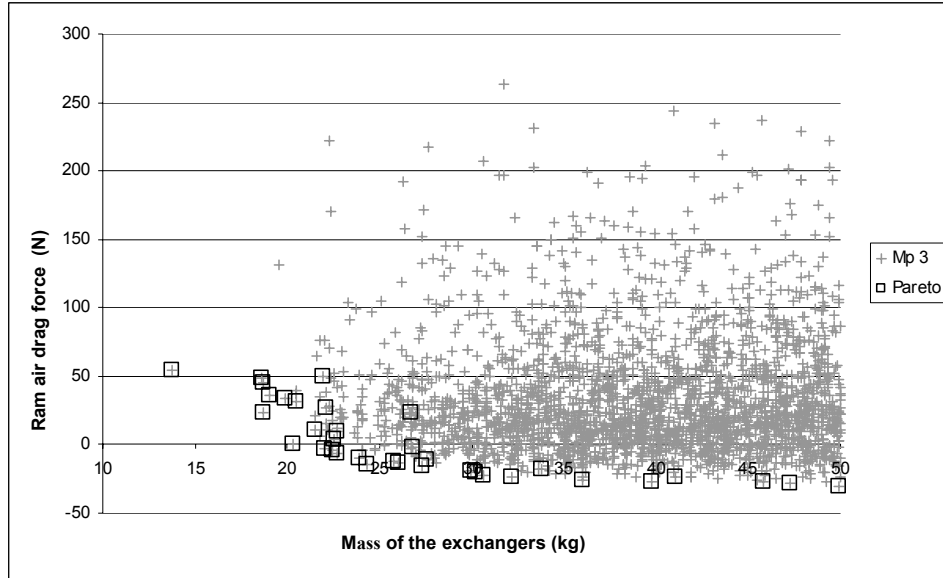
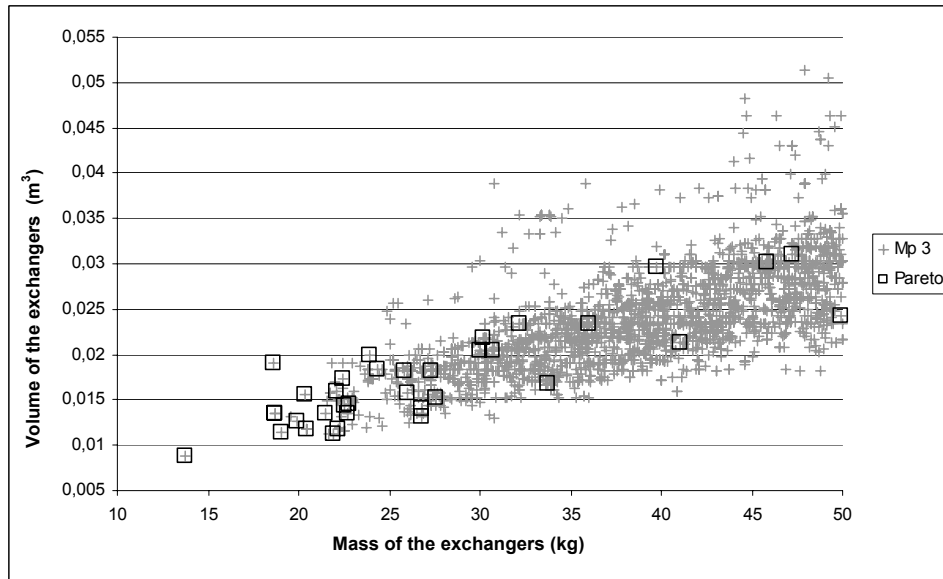


Figure 6 Performance space (mass versus volume) and Pareto set



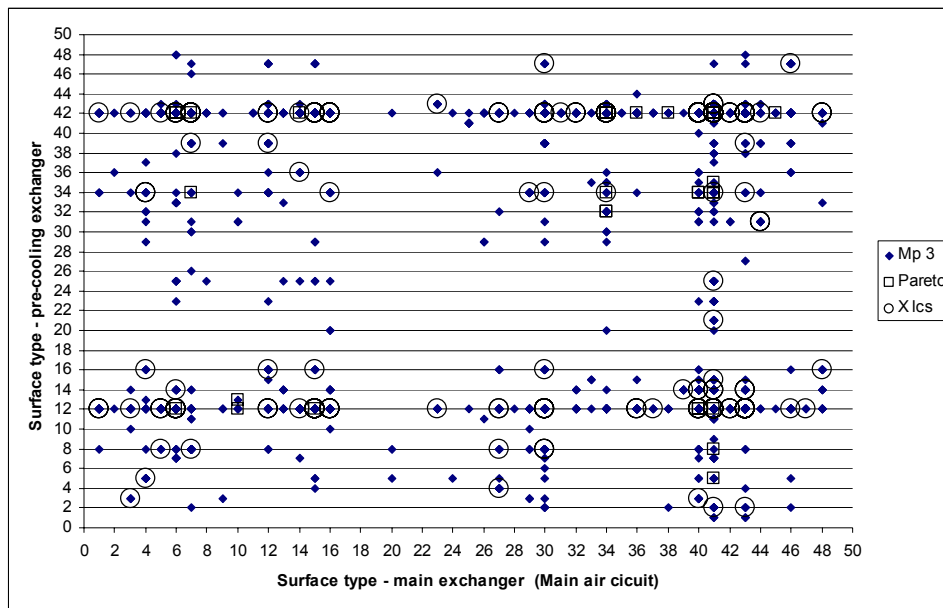
The Pareto set is located at the frontier of the solution space when displaying the solutions according to mass versus drag and mass versus volume (Figures 4 and 5). The reduction of the solution space and its visualisation within the performance space facilitates the choice between feasible design configurations.

4.2 Design space exploration and decision support

Despite the reduction of the solution space, design decisions remain difficult. To overcome this difficulty, we propose to supply designers with an overview of the design space: the solutions are displayed according to combined DVs to assist designers in making choices among them.

Figures 7 and 8 display the solutions (for $M_p = 0.3$) in the design space, according to the fin types of the two heat exchangers (main and precooling exchanger). Figure 7 concerns the main air circuit and Figure 8, the ram air circuit.

Figure 7 Design space and visualisation of relevant designer variable values (surface type) for main air circuit (see online version for colours)



We can observe in Figures 7 and 8 that there are few relevant fin combinations. In spite of 2634 solutions, the design space is not much filled. Thus, several solutions use the same fin combinations.

Designers can easily identify the relevant combinations for each circuit and the fin types which do not match any solution. For example, type 7 is relevant for the precooling exchanger on the ram air circuit as many embodiment design solutions use this surface type; many of them are nondominated solutions (see Figure 8).

Moreover, the identification of efficient surfaces is facilitated by highlighting the Pareto solutions and the solutions compatible with several life cycle stages (called 'X-lcs' in Figures 7 to 9). The Pareto solutions are the design solutions managing the best compromise between the requirements (minimising the drag, mass and volume of exchangers). These solutions are shown in Figures 7 to 9 to put emphasis on the optimal associations of fin types. Even if Pareto solutions and solutions functioning in many life cycle stages do not match, we can see that they use the same fin combinations; consequently, they differ in the values of other DVs.

Figure 8 Design space and visualisation of relevant design variable values (surface type) for ram air circuit (see online version for colours)

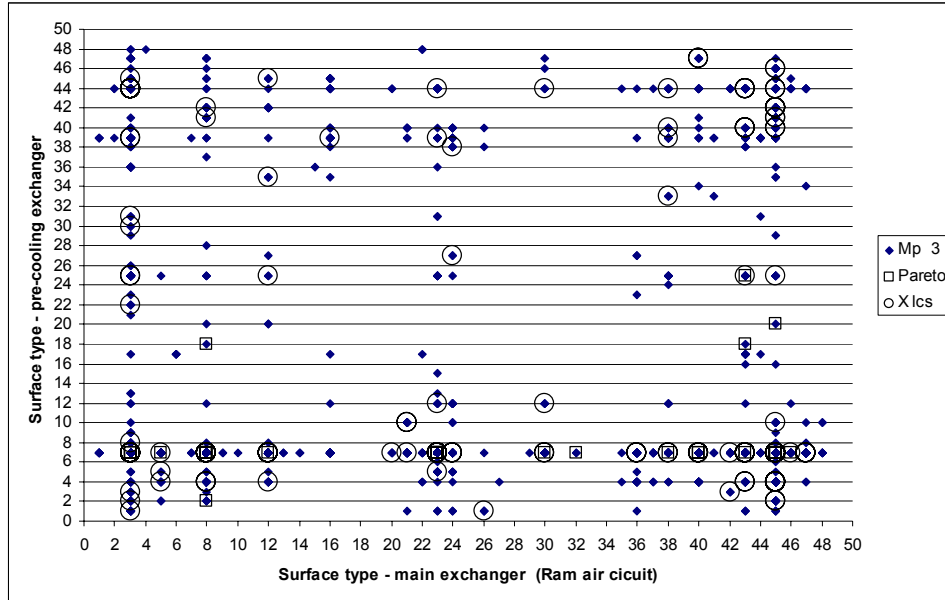
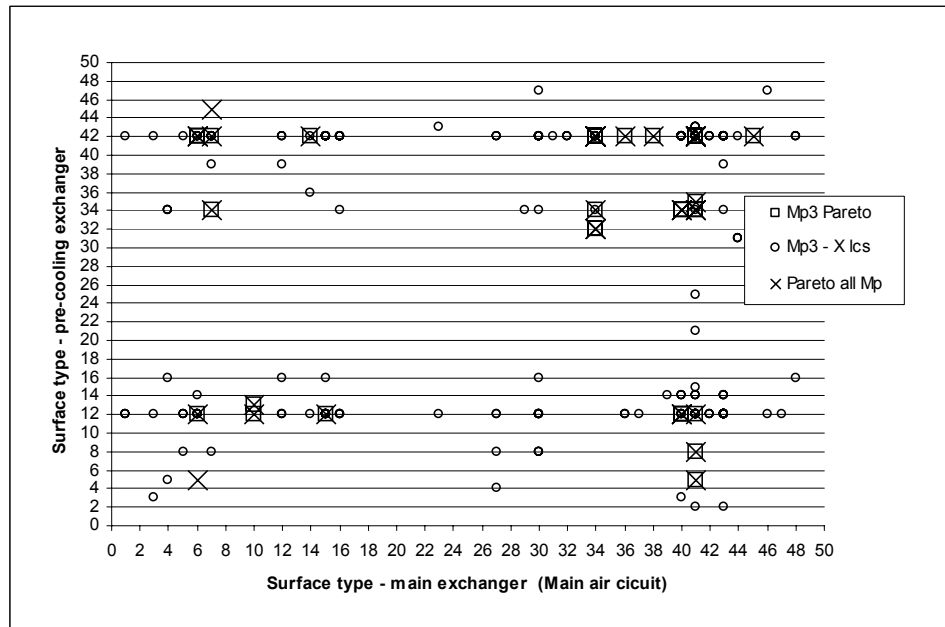


Figure 9 Visualisation of relevant fin combinations for the main air circuit and Pareto set for all of the solutions (all Mp's)



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Some fin types are well adapted to the definition of design solutions, but they are different for each circuit:

- For the main exchanger, fin type 41 is the most appropriate for the main air circuit and fin type 45 appears to be well adapted to the ram air circuit.
- For the precooling exchanger, fin types 12 and 42 may be used in the main air circuit, whereas fin type 7 is more adapted to the ram air circuit.

The intersection of these configurations of fins jointly belongs to the Pareto set and to the X-lcs set; for example, fin type 41 (main exchanger) is related to type 12 (precooling exchanger) for the main air circuit (see Figure 9).

Finally, some types of fins do not match any design solution and, therefore, seem to be irrelevant for the bootstrap application. For instance, whatever the air circuit being considered, types 17 to 19 are never involved in the functioning of the main heat exchanger.

These observations are confirmed by Figure 9, which superposes, on the solutions selected for $M_p = 0.3$, the Pareto set obtained for all the solutions (all M_p 's, *i.e.*, 5636 solutions). The Pareto set for $M_p = 0.3$ matches the Pareto set for every value of M_p (all M_p 's).

The preceding analysis cannot guide designers to the optimal solution of the bootstrap design problem. However, this investigation supports designer decisions by suggesting relevant guidelines and avoiding some irrelevant choices. These visualisations show that few fin types are well adapted to one particular air circuit and one particular exchanger. In particular, it supports designers in the process of choosing the fins. This choice highly influences the system functioning and is difficult to know *a priori*. Besides, we can see that the relevant types are not the same ones for the two circuits, which are functioning under different conditions.

Finally, a small number of DV configurations meets the whole of the design constraints for the various flight phases. This consideration corroborates the difficulty of finding design solutions suitable for the complete bootstrap life cycle; this difficulty appears to be the bottleneck of the bootstrap design process.

5 Conclusions

In this paper, the design of an aircraft air-conditioning system has been discussed. This air-conditioning system is based on a Joule-Brayton cycle, including a turbo engine and two heat exchangers. Designers are faced with the complexity and the coupling of physical phenomena inside this system. More to the point, the system must run during four flight phases corresponding to different pressures and temperatures of the air outside of the aircraft. Due to the complexity and the large size of the design exploration space, classical design processes are based on the investigation of a small number of design configurations.

In this paper, a wide design space ($1.04 \cdot 10^{15}$ design configurations) has been explored without considering *a priori* choices. This digital approach is based on GAs. Based on the selection, mutation and crossing of design solution principles, the exploration is performed by improving the satisfaction of the constraints of the design problem. The design problem is regarded as a CSP and a design solution must satisfy every constraint of the design problem.

This approach has proved to be influenced by some genetic parameters, mainly the mutation probability. Due to the coupling of the physical phenomena inside the air-conditioning system, the solving of the CSP appears to converge towards numerous solutions for high values of the mutation probability (30% to 60%). Despite the fact that the computing process converges towards 5636 feasible embodiment design solutions (1 hour of calculation), a few configurations proved to be adapted to the complete design problem; namely, a design problem facing several life cycle situations (several flight points).

Such an approach may be relevant to designing complex industrial systems or when the life cycle of the system is faced with varying situations. It supports designers in the process of determining feasible embodiments: designers can make decisions based on the identification of relevant or irrelevant values of the DVs. These decisions are also based on the management of the compromise between the design requirements. However, it has been observed that optimal solutions according to one particular life cycle situation may be unrelated to optimal solutions according to several life cycle situations.

Our perspectives concern the development of new operators inside GAs suitable for improving the robustness of the design solutions and for improving the performance of the solver with regard to the CSP paradigm. The CSP paradigm aims at separating knowledge (design constraints) and programming (solving methods).

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